## Foundations of Artificial Intelligence

## Perceptrons and Optimal Hyperplanes

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## Example: Majority-Vote Function

## Definition: Majority-Vote Function f<sub>majority</sub>

- $\label{eq:static-state} \begin{array}{l} \ N \ \text{binary attributes, i.e. } x \in \{0,1\}^N \\ \ \text{If more than } N/2 \ \text{attributes in } x \ \text{are true, then } f_{majority}(x) = 1, \\ \text{else } f_{majority}(x) = -1. \end{array}$
- How can we represent this function as a decision tree? - Huge and awkward tree!
- Is there an "easier" representation of f<sub>majority</sub>?























	<i>x</i> <sub>1</sub>	$x_2$	<i>x</i> <sub>3</sub>	<i>x</i> <sub>4</sub>	<i>x</i> <sub>5</sub>	<i>x</i> <sub>6</sub>	<i>x</i> <sub>7</sub>	у
Example 1	1	0	0	1	0	0	0	1
Example 2	1	0	0	0	1	0	0	1
Example 3	0	1	0	0	0	1	0	-1
Example 4	0	1	0	0	0	0	1	-1
	<i>w</i> <sub>1</sub>	w2	<i>w</i> <sub>3</sub>	w4	w <sub>5</sub>	w <sub>6</sub>	w <sub>7</sub>	b
Hyperplane 1	1	1	0	0	0	0	0	2
Hyperplane 2	0	0	0	1	1	-1	-1	0
Hyperplane 3	1	-1	1	0	0	0	0	0
Hyperplane 4	1	-1	0	0	0	0	0	0
	0.05	0.05	0	0.05	0.05	0.05	0.05	0