

CS 412
Introduction to Compilers
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Lecture 27: Dataflowanalysis 6 Apr 01

## Dataflow analyses

- Live variable analysis - register allocation, dead-code elimination
- Reaching definitions: what points in program does each variable definition reach? - copy, constant propagation
- Available expressions: which expressions computed earlier still have same value? - common sub-expression elimination

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## Quadruples

- Quadruple sequence is control flow graph (flowgraph)
- Nodes in graph: quadruples (not assembly statements)
- Edges in graph: ways to transfer control between quadruples (including fall-through)
- For node $n$, use[n] is variables used, $\operatorname{def}[n]$ is variables defined (assigned)
- Can generate directly from AST


## IR for data-flow analysis

- Tree IR: good for instruction selection, not so good for dataflow analysis
- Can flatten tree representation into simple nodes ( $a, b, c$ temps, labels L)
$\operatorname{MOVE}(a, O P(b, c))$
$\operatorname{MOVE}(a, \operatorname{MEM}(b))$ $a=b$ OP $c$
$a=[b]$
MOVE (a, MEM(b)) $a=[b]$
$[a]=b$
$\operatorname{MOVE}(\operatorname{MEM}(a), b)$
J UMP(L) [a] $=b$
goto $L$
CJ UMP(a, L1, L2)
if a goto L1 else L2
LABEL(L)
$\operatorname{MOVE}(a, \operatorname{CALL}(f, \ldots))$
$\mathrm{L}:$
$\mathrm{a}=$
a
$\operatorname{EXP}(\mathrm{a}, \operatorname{CALL}(\mathrm{f}, \ldots)$.
$a=f(\ldots)$
f(...)
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## Converting to quadruples

- Conversion is tree simplification that aggressively adds new temporaries



## Def \& Use

n
$a=b$ OP c a $\quad$ b, $c$

| $a=[b]$ | $a$ | $b$ |
| :--- | :--- | :--- |
| $[a]=b$ | $a, b$ |  |

goto L
if a goto L1 else goto L2
$a=f(\ldots)$
f(...)
a
(

## Converting back to tree

- Convert quadruples to simple trees
- Look for temporaries in statement sequence used and defined only once
- Move definition just before use
- Glue tree, eliminating temporary
$t=c * a$
$a=\ldots+t$$\triangleleft \begin{gathered}\operatorname{MOVE}(t, *(c, a)) \\ \operatorname{MOVE(a,+(b,t))}\end{gathered} \Rightarrow \operatorname{MOVE(a,+(b,*(c,a)))}$
- Requires dataflow analyses to do right (reaching definitions, available expressions)

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## Live variable analysis

- Useful even for IR: dead code elimination
- Output: in[n] and out[n] associated with every node $n$ in flowgraph
- Constraints:
in[n] $\supseteq$ use[n]
$\operatorname{in}[n] \cup \operatorname{def}[n] \supseteq$ out[n]
out $[n] \supseteq$ in[ $\left.n^{\prime}\right]$ for all successors $n^{\prime}$ of $n$
- Dataflow equations:
$\operatorname{in}[n]=u s e[n] \cup(o u t[n]-\operatorname{def}[n])$
$\operatorname{out}[\mathrm{n}]=\cup_{\mathrm{n}^{\prime}} \operatorname{in}\left[\mathrm{n}^{\prime}\right]$
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## Reaching definitions analysis

- Question: what uses in program does a given variable definition reach?
- Used for constant propagation, copy propagation
- if only one definition reaches a particular use, can replace use by definition
- copy propagation requires that copied value still has same value - use available expressions
- Input: flowgraph
- Output: in[n], out[n] is set of nodes defining some variable such that defn may reach beginning, end of $n$


## Reaching definitions



## Gen, kill

- Define: $\operatorname{defs}(x)$ is set of nodes defining var $x$
- Define: gen[n], kill[n]

| $n$ | gen[n] | kill[n] |
| :--- | :--- | :--- |
| $a=b$ OP c |  |  |
| $a=[b]$ | $\{n\}$ | $\operatorname{defs}(a)-\{n\}$ |
| $[a]=b$ | $\{n\}$ | $\operatorname{defs}(a)-\{n\}$ |
| goto L | $\}$ | $\}$ |
| if a goto L1 else goto L2 | $\}$ | $\}$ |
| L: | $\}$ | $\}$ |
| $a=f(\ldots)$ | $\{n\}$ | $\}$ |
| $f(\ldots)$ | $\}$ | $\operatorname{defs}(a)-\{n\}$ |
|  |  | $\}$ |

## Data-flow equations

$$
\begin{aligned}
& \operatorname{in}\left[n^{\prime}\right]=\cup_{n \in \operatorname{prev}\left[n^{\prime}\right]} \operatorname{out}[n] \\
& \operatorname{out}[n]=\operatorname{gen}[n] \cup(\operatorname{in}[n]-\operatorname{kill}[n])
\end{aligned}
$$

- Algorithm: init in[n], out[n] with empty sets, apply equations as assignments until no progress (usual representation: bit vector)
- Eventually all equations satisfied
- Will terminate because in[n], out[n] can only grow, can be no larger than set of all defns
- Finds minimal solution to constraint eqns: accurate
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## du-, ud-chains



## Webs

- Register allocation by webs avoids false conflicts
int i;

$$
\text { for }(i=0 ; i \triangleleft n ; i++)\{\ldots\}
$$

$$
\text { for }(i=0 ; i \subset n ; i++)\{\ldots\} \text { no use/def pairs! }
$$

- Two different webs: can allocate i to two different registers


## Forward vs. Backward

- Liveness: backward analysis

```
in[n] =use[n] \cup (out[n] - def [n])
    out[n] = U Un'\in suoc[n] in[n']
```

- Reaching definitions: forward analysis
out[n] $=\operatorname{gen}[n] \cup($ in[n] - kill[n] $)$ $\operatorname{in}\left[\mathrm{n}^{\prime}\right]=\cup_{\mathrm{n} \in \operatorname{prev}\left[\mathrm{n}^{\prime}\right]}$ out[n]


## Available expressions

- Idea: want to perform common subexpression elimination

$$
\begin{gathered}
a=x+1 \\
\ldots \\
b=x+1
\end{gathered} \quad \square \begin{gathered}
a=x+1 \\
\ldots=a
\end{gathered}
$$

- Transformation is safe if original $x+1$ is an available expression (still computes same value)


## Register allocation

1. use reaching definitions to compute all related uses and defs
2. compute disjoint webs, rename all temporaries to their web names
3. run register allocation as before : fewer interfering temporaries

## Dataflow analysis

- Many dataflow analyses characterized simply by
- forward vs. backward analysis
- gen[n]
- kill[n]
- Use of intersection vs. union when combining data from several nodes (operator 7 )
out[n] $=\operatorname{gen}[n] \cup(i n[n]-\operatorname{kill}[n])$
$\operatorname{in}\left[\mathrm{n}^{\prime}\right]=\Pi_{\mathrm{n} \in \operatorname{prev}\left[\mathrm{n}^{\prime}\right]}$ out[n]


## Dataflow values

- Let in[n], out[n] be sets of nodes whose computed expression is available at n



## Constraints

```
out[n] \supseteq gen[n]
```

"An expression made available by n at least reaches n's output"
$\operatorname{in}\left[\mathrm{n}^{\prime}\right] \subseteq$ out $[\mathrm{n}]$ (if $\mathrm{n}^{\prime}$ is succ. of n )
"An expression is available at n ' only if it is available at every predecessor n"
out $[n] \cup$ kill[ $n] \supseteq \operatorname{in}[n]$
"An expression available on input is either available on output or killed"

## Summary

- Tree IR makes dataflow more difficult
- Saw reaching definitions, available expressions analyses
- How to use reaching definitions for better register allocations via webs
- Next time: a theory to explain why iterative solving works

