

JavaHyperText material

Look at entries

spanning This one gives you a .zip file that contains a Java app to create random mazes.

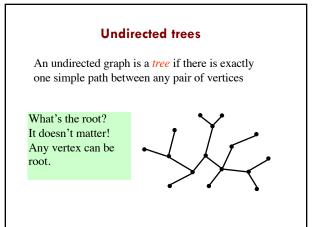
greedy

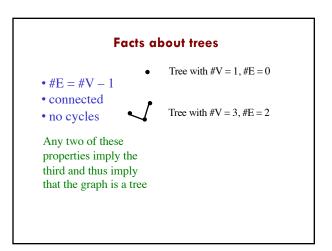
We go over two algorithms for generating a spanning tree of a graph. You have to know them only at a high level of abstraction.

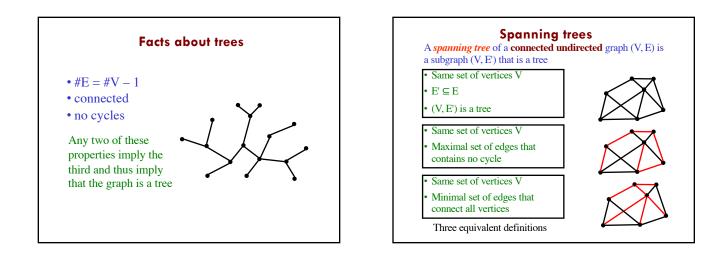
Amortized time

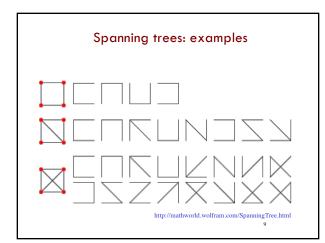
Visit JavaHyperText, put "amort" into Filter Field, read the first ---one-page--- pdf file. In A5 –Heap.java, insert takes *amortized* time O(1).

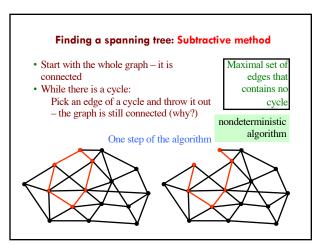
WHAT DOES THAT MEAN?

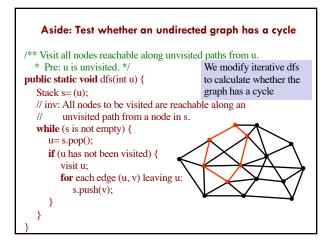


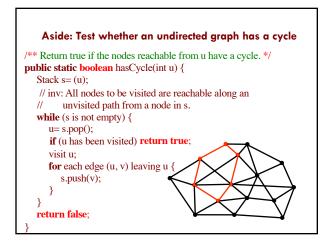


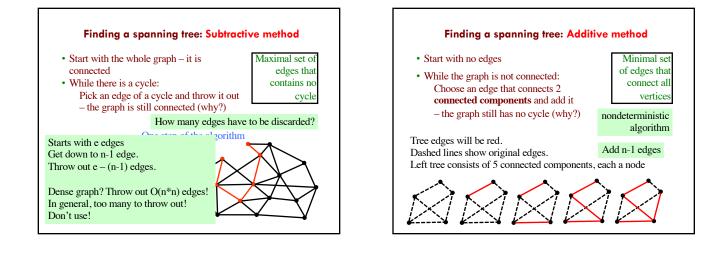






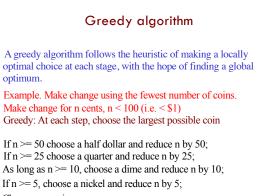








- Suppose edges are weighted (> 0)
- We want a spanning tree of *minimum cost* (sum of edge weights)
- Some graphs have exactly one minimum spanning tree. Others have several trees with the same minimum cost, each of which is a minimum spanning tree
- Useful in network routing & other applications. For example, to stream a video



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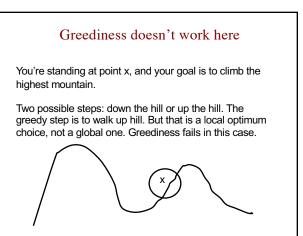
Choose n pennies.

Greediness works here

You're standing at point x. Your goal is to climb the highest mountain.

Two possible steps: down the hill or up the hill. The greedy step is to walk up hill. That is a local optimum choice, not a global one. Greediness works in this case.





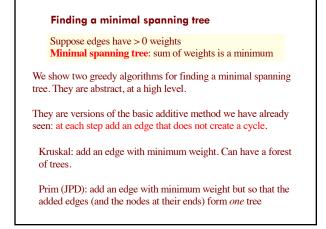
Greedy algorithm —doesn't always work!

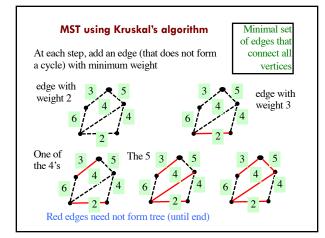
A greedy algorithm follows the heuristic of making a locally optimal choice at each stage, with the hope of finding a global optimum. Doesn't always work

Example. Make change using the fewest number of coins. Coins have these values: 7, 5, 1 Greedy: At each step, choose the largest possible coin

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Consider making change for 10. The greedy choice would choose: 7, 1, 1, 1. But 5, 5 is only 2 coins.





Kruskal Start with the all the nodes and no edges, so there is a forest of trees, each of which is a single node (a leaf).

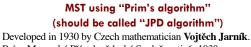
Minimal set of edges that connect all vertices

At each step, add an edge (that does not form a cycle) with minimum weight

We do not look more closely at how best to implement Kruskal's algorithm —which data structures can be used to get a really efficient algorithm.

Leave that for later courses, or you can look them up online yourself.

We now investigate Prim's algorithm

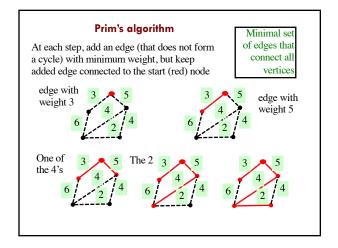


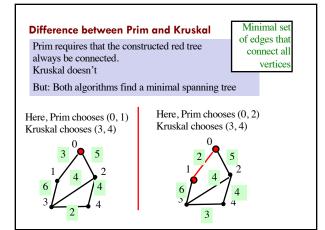
Práce Moravské Přírodovědecké Společnosti, 6, 1930, pp. 57–63. (in Czech)

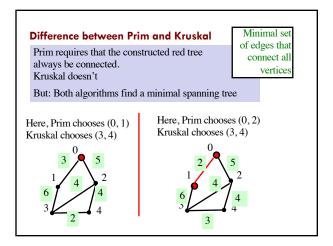
Developed in 1957 by computer scientist **Robert C. Prim**. *Bell System Technical Journal*, 36 (1957), pp. 1389–1401

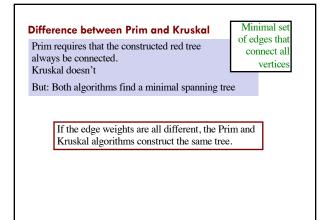
Developed about 1956 by **Edsger Dijkstra** and published in in 1959. *Numerische Mathematik* 1, 269–271 (1959)

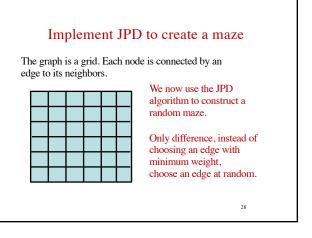


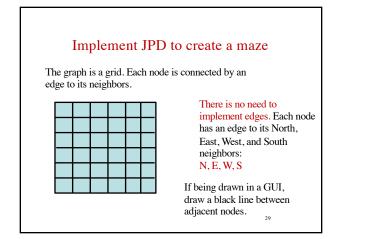


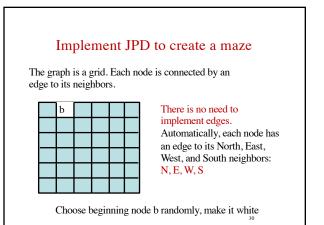


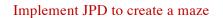




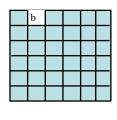








The graph is a grid. Each node is connected by an edge to its neighbors.

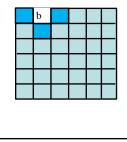


All nodes that have been added to the spanning tree are white. They have in them a letter b, N, E, W, or S ---as will be seen later.

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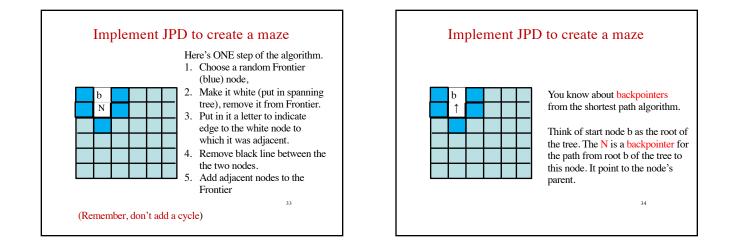
Implement JPD to create a maze

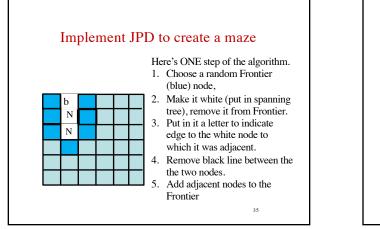
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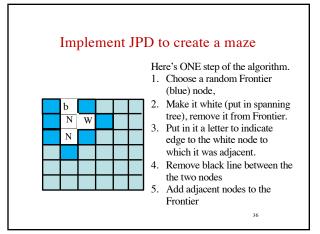


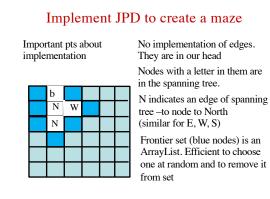
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The frontier set are nodes that are adjacent to white nodes. They are in an ArrayList F. We make them blue. 32

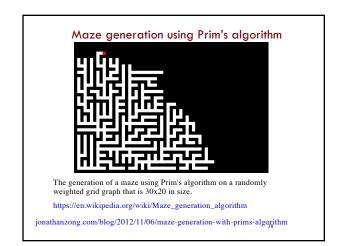


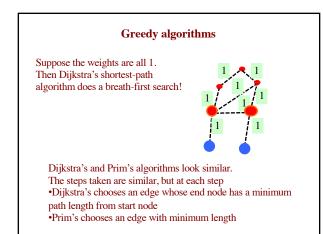






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Greedy algorithm: An algorithm that uses the heuristic of making the locally optimal choice at each stage with the hope of finding the global optimum.

Dijkstra's shortest-path algorithm makes a locally optimal choice: choosing the node in the Frontier with minimum L value and moving it to the Settled set. And, it is proven that it is not just a hope but a fact that it leads to the global optimum.

Similarly, Prim's and Kruskal's locally optimum choices of adding a minimum-weight edge have been proven to yield the global optimum: a minimum spanning tree.

BUT: Greediness does not always work!

