SEPARATION OF CONCERNS

Term used by Edsger Dijkstra in discussing the development of algorithms and mathematical proofs.

Rarely discussed, but its use is crucial in some situations.

Illustrate with the development of bubble down.

/** class invariant –array b, integer size, HashMap map— is true, except that b[k] may be out of place.

Bubble b[k] down. */
public void bubbleDown(int k)

```
int cR = 2 * k + 2; int cL = 2 * k + 1;
                                                    Simplicity
while (cL \leq size && cR \leq size + 1) {
  if (compareTo(cL, cR) == 0) { // same priority for left and right
     if (compareTo(k, cL) \leq 0) {
        swap(cR, k); k = cR;
        cR = 2 * k + 2; cL = 2 * k + 1;
     } else if (compareTo(k, cL) \geq= 0) { return; }
  } else if (compareTo(cL, cR) > 0 || !map.containsValue(cR) && ...) {
        // left has higher priority, or just left exists
        if (compareTo(k, cL) < 0) {
          swap(cL, k); k = cL;
          cR = 2 * k + 2; cL = 2 * k + 1;
        } else if (compareTo(k, cL) \geq= 0) { return; }
  } else if (compareTo(cR, cL) > 0 || !map.containsValue(cL) && ...) {
        // right has higher priority, or just right exists
        if (compareTo(k, cR) \leq 0) {
          swap(cR, k); k = cR;
        cR = 2 * k + 2; cL = 2 * k + 1;
  } else if (compareTo(k, cR) \geq= 0) { return; }
```

```
// inv: class invariant is true except k may be out of place while (2k+1 < size && k belongs below a child ) { bubble down
```

}

Checking k belongs below a child requires a lot of initialization, perhaps a helper method. It may require knowing which child to bubble. But that's another concern!

Try developing without it here!

Concerns:

When to stop bubbling:

- 1. k has no children.
- 2. ! k belongs below a child.

Which child to bubble with? How to do the bubbling?

```
// inv: class invariant is true except k may be out of place
while ( 2*k+1 < size) {
   // bubble down if possible, return if not</pre>
```

}

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```
// inv: class invariant is true except k may be out of place
while ( 2*k+1 < size) {
    //Set c to the child to bubble with
    int c= 2*k+1; // left child
    if (c+1 < size && compareTo(c+1, c) >= 0) c= c+1;
}
```

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if (compareTo(k, c) >= 0) return;
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How to do the bubbling?

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// inv: class invariant is true except k may be out of place
while (2*k+1 < size) {
   //Set c to the child to bubble with
   int c= 2*k+1; // left child
   if (c+1 < size \&\& compareTo(c+1, c) >= 0) c= c+1;
   if (compareTo(k, c) \geq 0) return;
   swap(k, c);
   k = c;
```

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How to do the bubbling?