

Lecture 16: More Recursion!

CS 1110

Introduction to Computing Using Python

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Announcements

- Prelim 1 accounts for 15% of course grade only. Treat it as a diagnostic tool: is there a topic that you need to review? Strengthen your foundation now. 1-on-1 meeting opportunities to be available on CMS soon
- Attend your lab session! *New experiment:* you can additionally attend another online lab session to get more help on weekly lab exercises
- ACSU annual Research Night, Apr 8 5:30-7:30pm
 Interested in undergraduate research in CS?
 - https://discord.com/invite/cCM3QuGY3B

Recursion

Recursive Function:

A function that calls itself (directly or indirectly)

Recursive Definition:

A definition that is defined in terms of itself

From previous lecture: Factorial

Non-recursive definition:

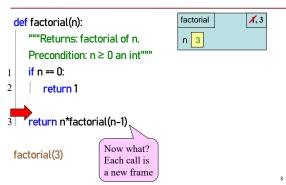
 $n! = n \times n-1 \times \dots \times 2 \times 1$ $= n (n-1 \times \dots \times 2 \times 1)$

Recursive definition:

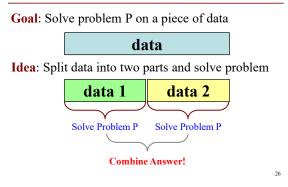
n! = n (n-1)! for n > 0 Recursive case 0! = 1 Base case

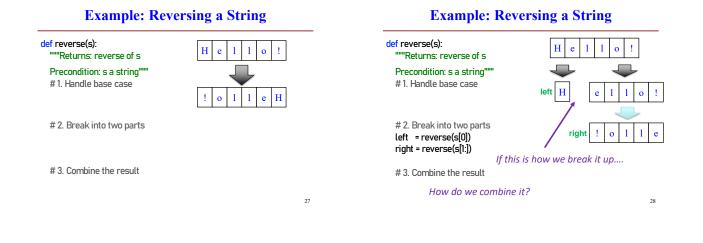
Recursion

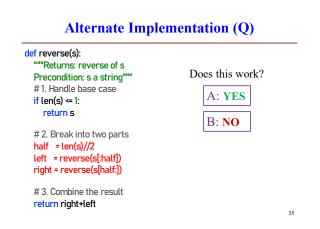
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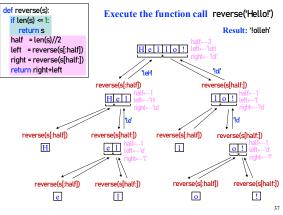


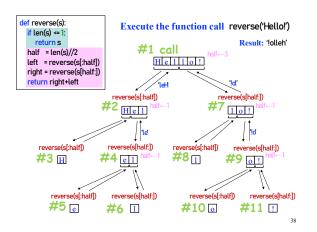
Divide and Conquer

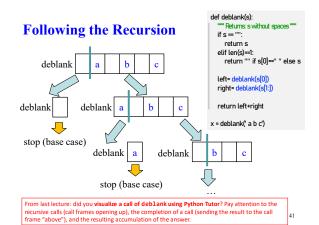












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Example: Palindromes

• Example:

AMANAPLANACANALPANAMA

MOM

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- Dictionary definition: "a word that reads (spells) the same backward as forward"
- Can we define recursively?

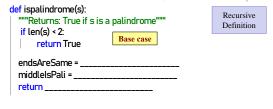
Example: Palindromes

- String with ≥ 2 characters is a palindrome if:
- its first and last characters are equal, and
- the rest of the characters form a palindrome
- Example: have to be the same
 - AMANAPLANACANALPANAMA
- has to be a palindrome
 Implement: def ispalindrome(s):
 """Returns: True if s is a palindrome""

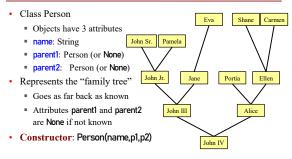
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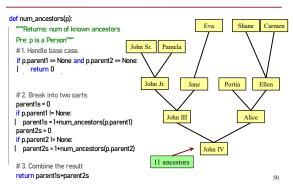
Recursion and Objects



def num ancestors(p): Shane Carmen Eva "Returns: num of known ancestors Pre: p is a Person" John Sr. Pamela #1. Handle base case # No parents # (no ancestors) John Jr. Jane Portia Eller # 2. Break into two parts # Has parent1 or parent2 # Count ancestors of each one John III # (plus parent1, parent2 themselves) John IV 11 ancestors # 3. Combine the result 49

Recursion and Objects

Recursion and Objects



Recursion and Objects

def num_ancestors(p):

"""Returns: num of known ancestors Pre: p is a Person"""

#1. Handle base case. if p.parent1 == None and p.parent2 == None: | return 0

#2. Break into two parts parent1s = 0 if p.parent1 != None: | parent1s = 1+num_ancestors(p.parent1s) parent2s = 0 if p.parent2s = 1+num_ancestors(p.parent2s) | parent2s = 1+num_ancestors(p.parent2s)

3. Combine the result return parent1s+parent2s We don't actually need this. It is handled by the conditionals in #2.

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Exercise: All Ancestors

