

CS412/413

Introduction to Compilers and Translators Spring '00

Lecture 6: LR grammars and automatic
parser generators

Outline

- Review of shift-reduce parsers
- Limitations of LR(0) grammars
- SLR, LR(1), LALR parsers
- parser generators

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Administration

- Programming Assignment 1 due now!
- Homework 2 due in 1 week
- Programming Assignment 2 due in 2 + ϵ weeks

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Bottom-up parsing

- Apply productions *backwards* as *reductions*
- Builds parse tree from terminal symbols up towards start symbol
- Shift-reduce parser constructs right-most derivation using sequence of *shift* and *reduce* operations

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Shift-reduce parsing

- Parsing is a sequence of *shifts* and *reduces*
- **Shift** -- push look-ahead token onto stack

stack	input	
(1+2+(3+4))+5	shift 1
(1	+2+(3+4))+5	

- **Reduce** -- Replace symbols γ in top of stack with non-terminal symbol X , corresponding to production $X \rightarrow \gamma$ (pop γ , push X)

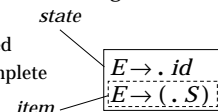
stack	input	
(S+E	+(3+4))+5	reduce $S \rightarrow S+E$
(S	+(3+4))+5	

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LR(0) states

- **Problem: when to reduce & what production?**
- Idea: state summarizes parser stack prefix, keeps track of what productions might need to be the next reduce
 - what tokens can be shifted
 - when a production is complete
- A state is a set of *items*: partially completed productions that might appear in derivation

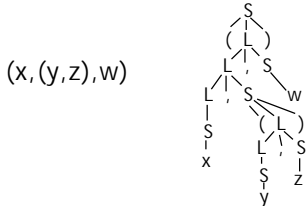


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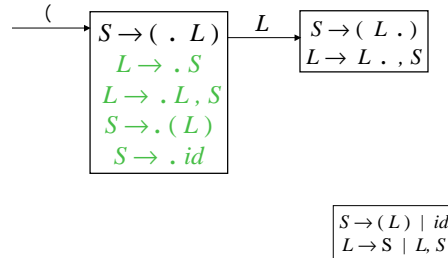
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An LR(0) grammar: lists

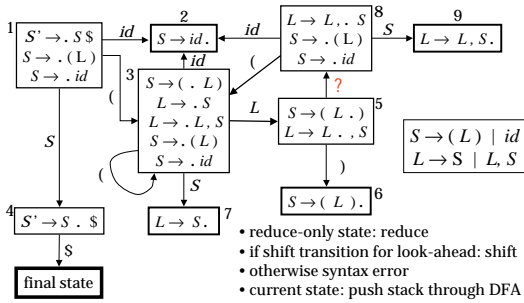
$S \rightarrow id \mid (L)$
 $L \rightarrow L, S \mid S$



Constructing states



Full DFA (Appel p. 63)



Determining current state

- Run parser stack through the DFA
- State tells us what productions might be reduced next

stack	input	state = ?
((L,	x), y)	action = ?
((id,(?

Optimization

- Attach parser state to each stack entry
- Don't have to traverse DFA all over again after each reduction
- Just start from state at top of stack when RHS γ is removed, take single step for LHS non-terminal.

((L	, y)	state = 6
(S	, y)	state = ?

- Stack entries labeled w/state

derivation	stack	input	action
((x),y) ←	1	((x),y)	shift, goto 3
((x),y) ←	1 (3	(x),y)	shift, goto 3
((x),y) ←	1 (3 (3	x),y)	shift, goto 2
((x),y) ←	1 (3 (3 x ₂),y)		reduce S → id
((S),y) ←	1 (3 (3 S ₇),y)		reduce L → S
((L),y) ←	1 (3 (3 L ₅),y)		shift, goto 6
((L),y) ←	1 (3 (3 L ₅) ₆ ,y)		reduce S → (L)
((S),y) ←	1 (3 S ₇ ,y)		reduce L → S
(L,y) ←	1 (3 L ₅ ,y)		shift, goto 8
(L,y) ←	1 (3 L ₅ , 8 y)		shift, goto 9
(L,y) ←	1 (3 L ₅ , 8 y ₂)		reduce S → id
(L,S) ←	1 (3 L ₅ , 8 S ₉)		reduce L → L, S
(L) ←	1 (3 L ₅)		shift, goto 6
(L) ←	1 (3 L ₅) ₆		reduce S → (L)
S	1 S ₁	S	done

Implementation: LR parsing table

input (terminal) symbols

state	next action
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Action table
Used at every step to decide whether to shift or reduce

non-terminal symbols

state	next state
-------	------------

Goto table
Used only when reducing, to determine next state

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Shift-reduce parser table

terminal symbols

non-terminal symbols

state	next actions	next state on red'n
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Actions in table

- shift and goto state n
- reduce using $X \rightarrow \gamma$
 - pop symbols γ off stack
 - using state label of top (end) of stack, look up X in *goto table* and goto that state

- DFA + stack = push-down automaton (PDA)

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List grammar parse table

	()	id	,	\$	S	L
1	s3		s2			g4	
2	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$		
3	s3		s2			g7	g5
4					accept		
5			s6		s8		
6	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$		
7	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$		
8	s3		s2			g9	
9	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$		

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LR(0) Limitations

- An LR(0) machine only works if states with reduce actions have a *single* reduce action -- in those states, *always* reduce ignoring input
- With more complex grammar, construction gives states with shift/reduce or reduce/reduce conflicts
- Need to use look-ahead to choose

ok

$L \rightarrow L, S.$

shift / reduce

$L \rightarrow L, S.$
$S \rightarrow S, L$

reduce / reduce

$L \rightarrow S, L.$
$L \rightarrow L.$

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List grammar parse table

	()	id	,	\$	S	L
1	s3		s2			4	
2	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$	$S \rightarrow id$		
3	s3		s2			7	5
4					accept		
5			s6		s8		
6	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$	$S \rightarrow (L)$		
7	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$	$L \rightarrow S$		
8	s3		s2			9	
9	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$	$L \rightarrow L, S$		

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How about sum grammar?

$$S \rightarrow S + E / E$$

$$E \rightarrow \text{num} \mid (S)$$

- This is LR(0)
- Right-associative version isn't:

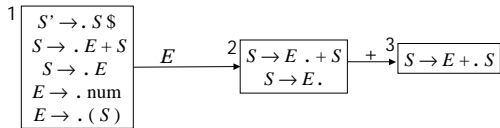
$$S \rightarrow E + S / E$$

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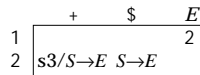
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LR(0) construction

$$\begin{aligned} S &\rightarrow E + S / E \\ E &\rightarrow \text{num} \mid (S) \end{aligned}$$



What to do on +?



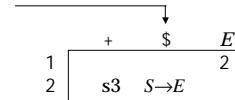
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SLR grammars

$$\begin{aligned} S &\rightarrow E + S / E \\ E &\rightarrow \text{num} \mid (S) \end{aligned}$$

- Idea: Only add reduce action to table if look-ahead symbol is in the *FOLLOW* set of the non-terminal being reduced
- Eliminates some conflicts
- $FOLLOW(S) = \{ \$,) \}$
- Many language grammars are SLR



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LR(1) parsing

- Gets as much power as possible out of 1 look-ahead symbol
- LR(1) grammar = recognizable by a shift/reduce parser with 1 look-ahead.
- LR(1) items keep track of look-ahead symbol expected to follow this production

LR(0): $S \rightarrow . S + E$

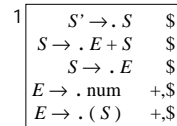
LR(1): $S \rightarrow . S + E \quad +$

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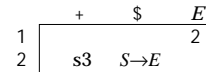
LR(1) construction

$$\begin{aligned} S &\rightarrow E + S / E \\ E &\rightarrow \text{num} \mid (S) \end{aligned}$$



Know what to do if:

- reduce look-aheads distinct
- not to right of any dot



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LALR grammars

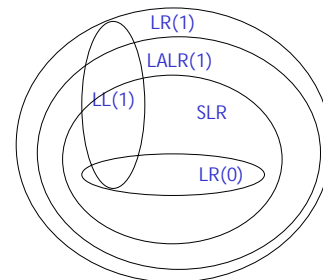
- Problem with LR(1): too many states
- LALR(1) (Look-Ahead LR)
 - Merge any two LR(1) states whose items are identical except look-ahead
 - Results in smaller parser tables -- works extremely well in practice

$$\begin{aligned} S &\rightarrow id . + \\ S &\rightarrow E . \$ \end{aligned} + \begin{aligned} S &\rightarrow id . \$ \\ S &\rightarrow E . + \end{aligned} = ?$$

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Classification of Grammars



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How are parsers written?

- Automatic parser generators: yacc, bison, CUP
- Accept LALR(1) grammar specification
- *plus*: declarations of precedence, associativity

Associativity

$$S \rightarrow S + E \mid E$$

$$E \rightarrow \text{num} \mid (S)$$



$$E \rightarrow E + E \mid \text{num} \mid (E)$$

What happens if we run this grammar through LALR construction?

Conflict!

$$E \rightarrow E + E \mid \text{num} \mid (E)$$

$E \rightarrow E + E \cdot$	+
$E \rightarrow E \cdot + E$	+, \$

shift/reduce conflict

$$1+2+3$$

^

shift: 1+(2+3)
reduce: (1+2)+3

Grammar in CUP

non terminal E; terminal PLUS, LPAREN...
precedence left PLUS:

"When shifting + conflicts with reducing a production containing +, choose reduce"

$E ::= E \text{ PLUS } E$
| LPAREN E RPAREN
| NUMBER ;

Precedence

- Also can handle operator precedence

$$E \rightarrow E + E \mid T$$

$$T \rightarrow T \times T \mid \text{num} \mid (E)$$



$$E \rightarrow E + E \mid E \times E$$

$$\mid \text{num} \mid (E)$$

Conflicts w/o precedence

$$E \rightarrow E + E \mid E \times E$$

$$\mid \text{num} \mid (E)$$

$E \rightarrow E \cdot + E$	any	$E \rightarrow E + E \cdot$	\times
$E \rightarrow E \times E \cdot$	+	$E \rightarrow E \cdot \times E$	any

Precedence in CUP

precedence left PLUS;
precedence left TIMES; // TIMES > PLUS
 $E ::= E \text{ PLUS } E \mid E \text{ TIMES } E \mid \dots$

$E \rightarrow E \cdot + E$	<i>any</i>
$E \rightarrow E \times E \cdot$	+

Rule: in conflict, choose
reduce if production
symbol higher precedence
than shifted symbol; choose
shift if vice-versa

$E \rightarrow E + E \cdot$	×
$E \rightarrow E \cdot \times E$	<i>any</i>

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Summary

- Look-ahead information makes SLR(1), LALR(1), LR(1) grammars expressive
- Automatic parser generators support LALR(1)
- Precedence, associativity declarations simplify grammar writing
- Can we use parsers for programs other than compilers?

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